

Name:

## QUIZ – MATH GRADE 10

1. (28%) Given the function  $f(x) = -3\cos(\frac{\pi}{3}x) - 4$ . Fill the blanks:

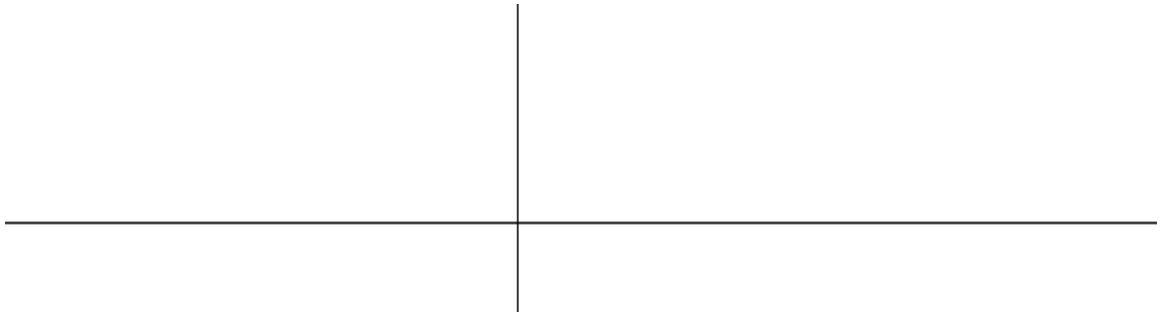
a. (2%) Amplitude = \_\_\_\_\_

c. (2%) Midline is: \_\_\_\_\_

b. (5%) Period = \_\_\_\_\_

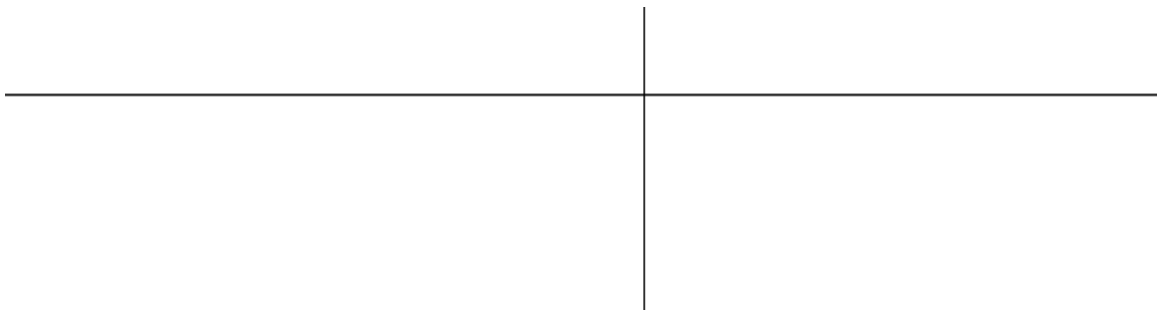
d. (4%) Range: \_\_\_\_\_

e. (6%) Sketch 1 period on each side of the y axis. **Indicate on the graph the coordinates of y int, x int max and min.**



f. (4%)  $g(x) = f(x-1) + 1 =$  \_\_\_\_\_

g. (5%) Sketch  $g(x)$ . **Write down the coordinates of y int, x int max and min.**



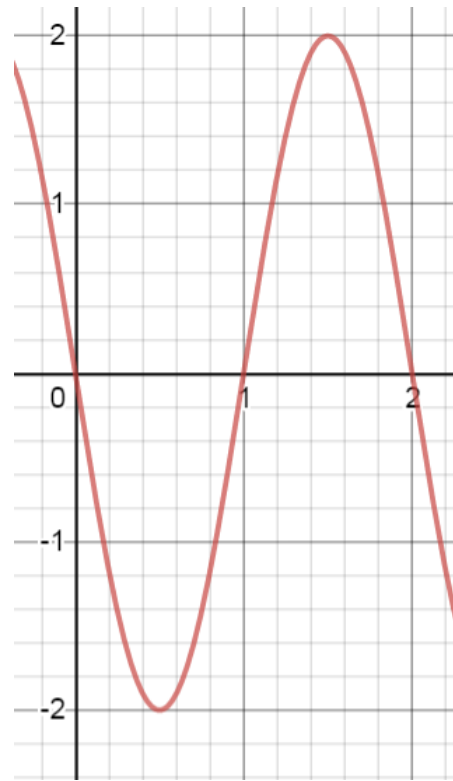
2. (20%) Given the function. Fill the blanks:

a. (2%) Amplitude = \_\_\_\_\_

b. (5%) Period = \_\_\_\_\_

c. (2%) Midline is: \_\_\_\_\_

d. (2%) Range: \_\_\_\_\_



e. (6%) The function can be written in the form  $f(x) = A\sin(a(x + b)) + c$

$A =$  \_\_\_\_\_

$a =$  \_\_\_\_\_

$b =$  \_\_\_\_\_

$c =$  \_\_\_\_\_

f. (3%) The function can be written in the form  $f(x) = A\cos(a(x + B)) + c$

$B =$  \_\_\_\_\_

3. (10%) Given the function  $f(x) = -10\cos\left(\frac{\pi}{112}(x + 33)\right) - 1$ . Determine the value of  $k$  for which the equation  $f(x) = k$  has no solutions.

4. (22%) A formula for the temperature  $T$  in  $^{\circ}\text{C}$  of an element in an experiment at a time  $t$  hours is

$$T(t) = A\sin(B(t - D)) + C,$$

It is known that on the graph the point  $(-2, -3)$  is a minimum point and the point  $(10, 9)$  is the following maximum point.

- (3%) Find the value of  $C$
- (3%) Find the value of  $A$
- (6%) Find the value of  $B$
- (3%) Show that the value of  $D$  is 4
- (3%) Find one instant in which the temperature decreases most rapidly.
- (4%) It is known that at  $t = 9$  h the temperature is  $k$ . Find the next 2 instants at which the temperature is  $k$ .

5. (20%) Given the function  $f(x) = 4\tan\left(\frac{\pi}{3}x\right)$ .

- (8%) Find its domain
- (6%) Find its  $x$  intercepts
- (6%) Write down the equation of 2 vertical asymptotes of the function

$$-f(x + 1) + 3$$

**BONUS (10%)**

The Temperature  $T(t)$  degrees, at  $t$  hours after midnight on a particular day is given by

$$T(t) = 3\sin(2t) + 5, \quad 0 \leq t \leq 4\pi$$

- (a) Find the maximum temperature and the minimum depth of the water. (2)

- (b) Find the values of  $t$  for which  $T(t) < 5$ . (4)

- (c) Find the values of  $t$  for which  $T(t) < 6.5$ . (4)