

Name:

QUIZ 26 – MATH IB HL

1. (27%) Given the function $f(x) = -3\sin\left(\frac{2\pi}{3}x\right) - 4$. Fill the blanks:

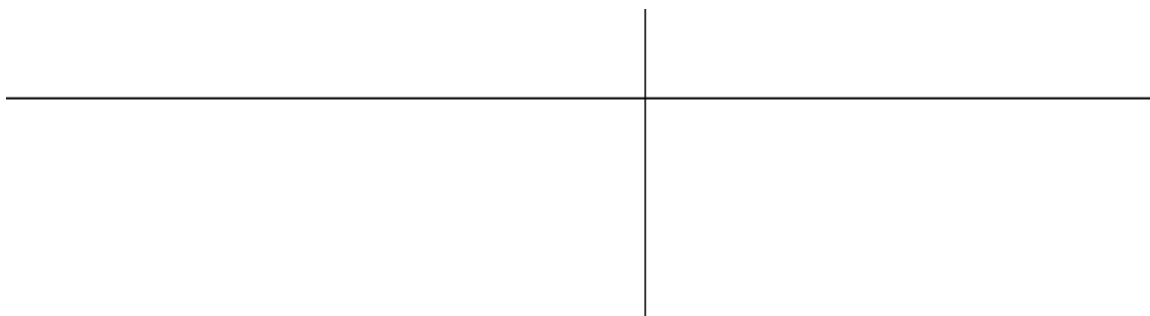
a. (2%) Amplitude = _____

c. (2%) Midline is: _____

b. (4%) Period = _____

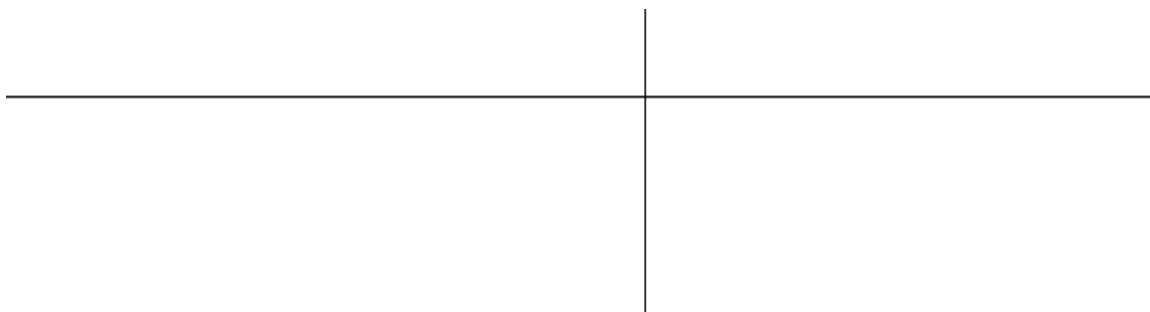
d. (4%) Range: _____

e. (6%) Sketch 1 period on each side of the y axis. Indicate on the graph the coordinates of y int, x int max and min.



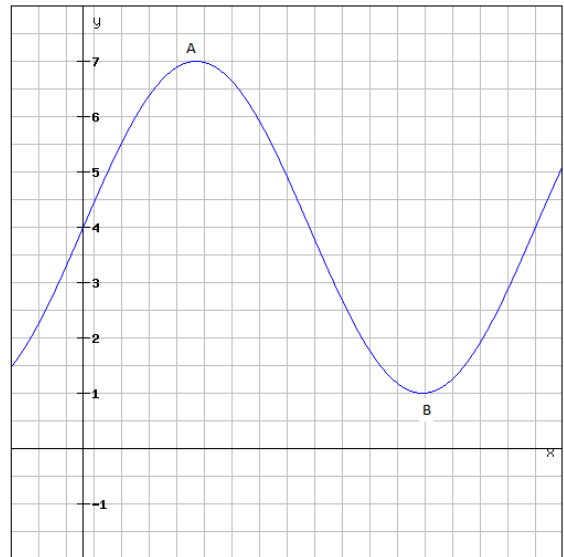
f. (4%) $g(x) = f(x - 1) + 1 =$ _____

g. (5%) Sketch $g(x)$ as the transformation of $f(x)$ sketched on the graph above. Write down the coordinates of y int, x int max and min.



2. (21%) Given the function. Point A $(\frac{3\pi}{2}, 7)$, Point B $(\frac{9\pi}{2}, 1)$ Fill the blanks:

- (2%) Amplitude = _____
- (4%) Period = _____
- (2%) Midline is: _____
- (3%) Range: _____



Fill the blanks:

- e. (5%) $f(x) = \underline{\hspace{1cm}} \cos(\underline{\hspace{1cm}}) \underline{\hspace{1cm}}$
- f. (5%) $f(x) = \underline{\hspace{1cm}} \sin(\underline{\hspace{1cm}}) \underline{\hspace{1cm}}$

3. (10%) Given the function $f(x) = 8\cos(\frac{7\pi}{22}(x-3.4)) - 7$. Determine the value of k for which the equation $f(x) = k$ has solutions.

4. (22%) A formula for the temperature T in $^{\circ}\text{C}$ of an element in an experiment at a time t hours is

$$T(t) = A\sin(Bt) + C, \quad 0 \leq t \leq 16$$

It is known that on the graph the point $(6, 2)$ is a minimum point and the point $(10, 8)$ is a maximum point.

- (3%) Find the value of C
- (3%) Find the value of A
- (5%) Find the value of B
- (5%) When does the temperature decrease most rapidly?
- (6%) It is known that at $t = 0.5$ h the temperature is k . Find the next 2 instants at which the temperature is k .

5. (20%) Given the function $f(x) = 2 \tan\left(\frac{\pi}{2}x\right)$.

- (8%) Find its domain
- (6%) Find its x intercepts
- (6%) Write down the equation of 1 vertical asymptote of the function

$$3f(x + 1)$$