## 2.2. - LINEAR FUNCTIONS

1. Given the function: $\mathrm{f}(\mathrm{x})=-5$

- Complete the following table:

| X | -5 | -4 | -3 | -2 | -1 | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{f}(\mathrm{x})$ |  |  |  |  |  |  |  |  |  |  |  |

- Sketch the points of the chart on a graph (use a ruler).
- State the domain of the function: $\qquad$
- State the $y$ intercept (sketched on the graph: $\qquad$ , _(_)
- State the $x$ intercept: $\qquad$ , )
- The function is increasing on the interval: $\qquad$
- The function is decreasing on the interval: $\qquad$
- Sketch the function of the graph used for the points initially drawn
- State the range of the function: $\qquad$


2. Given the function: $f(x)=x+3$

- Complete the following table:

| x | -5 | -4 | -3 | -2 | -1 | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{f}(\mathrm{x})$ |  |  |  |  |  |  |  |  |  |  |  |

- Sketch the points of the chart on a graph (use a ruler).
- State the domain of the function: $\qquad$
- State the $y$ intercept (sketched on the graph: ( $\qquad$ , $\qquad$ )
- State the $x$ intercept: ( $\qquad$ , $\qquad$ )
- The function is increasing on the interval: $\qquad$
- The function is decreasing on the interval: $\qquad$
- Sketch the function of the graph used for the points initially drawn
- State the range of the function: $\qquad$


3. Given the function: $f(x)=-2 x-5$

- Complete the following table:

| x | -5 | -4 | -3 | -2 | -1 | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{f}(\mathrm{x})$ |  |  |  |  |  |  |  |  |  |  |  |

- Sketch the points of the chart on a graph (use a ruler).
- State the domain of the function: $\qquad$
- State the $y$ intercept (sketched on the graph: ( $\qquad$ , _()
- State the $x$ intercept: ( $\qquad$ , $\qquad$ )
- The function is increasing on the interval: $\qquad$
- The function is decreasing on the interval: $\qquad$
- Sketch the function of the graph used for the points initially drawn
- State the range of the function: $\qquad$


4. Given the function: $f(x)=4 x-3$

- Complete the following table:

| x | -5 | -4 | -3 | -2 | -1 | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{f}(\mathrm{x})$ |  |  |  |  |  |  |  |  |  |  |  |

- Sketch the points of the chart on a graph (use a ruler).
- State the domain of the function: $\qquad$
- State the $y$ intercept (sketched on the graph: ( $\qquad$ , _()
- State the $x$ intercept: $\qquad$ , $\qquad$ )
- The function is increasing on the interval: $\qquad$
- The function is decreasing on the interval: $\qquad$
- Sketch the function of the graph used for the points initially drawn
- State the range of the function: $\qquad$


5. Given below are the equations for five different lines. Match the function with its graph.

| Function | On the graph |
| :---: | :---: |
| $\mathrm{f}(\mathrm{x})=20+2 \mathrm{x}$ |  |
| $\mathrm{g}(\mathrm{x})=4 \mathrm{x}+20$ |  |
| $\mathrm{~s}(\mathrm{x})=-30+2 \mathrm{x}$ |  |
| $\mathrm{a}(\mathrm{x})=60-\mathrm{x}$ |  |
| $\mathrm{b}(\mathrm{x})=-2 \mathrm{x}+60$ |  |


6. The general functions that describes a straight line is $\qquad$
7. We know a function is a straight line because $\qquad$
8. The y-intercept (also called vertical intercept), tells us where the line crosses the
$\qquad$ . The corresponding point is of the form ( , ).
9. The x -intercept (also called horizontal intercept), tells us where the line crosses the
$\qquad$ . The corresponding point is of the form ( , ).
10. If $m>0$, the line $\qquad$ left to right. If $\qquad$ the line decreases left to right.
11. In case the line is horizontal m is $\qquad$ and the line is of the form $\qquad$ .
12. The larger the value of $m$ is, the $\qquad$ the graph of the line is.
13. Given the graph, write, the slope (m), $b$ and the equation of the line:

$\mathrm{m}=\ldots \quad \mathrm{b}=\ldots \quad \mathrm{f}(\mathrm{x})=$

$\qquad$
$\mathrm{m}=$
$\mathrm{b}=$
$\mathrm{f}(\mathrm{x})=$

$\mathrm{m}=$ $\qquad$ $\mathrm{b}=$ $\qquad$ $\mathrm{f}(\mathrm{x})=$ $\qquad$
$\mathrm{m}=$ $\qquad$ $\mathrm{b}=$ $\qquad$ $f(x)=$

$\mathrm{m}=$ $\qquad$ $\mathrm{b}=$ $\qquad$ $f(x)=$

$\mathrm{m}=$ $\qquad$ $\mathrm{b}=$ $\qquad$ $\mathrm{f}(\mathrm{x})=$ $\qquad$


$$
\mathrm{m}=\ldots \quad \mathrm{b}=\ldots \quad \mathrm{f}(\mathrm{x})=
$$

$\qquad$ $\mathrm{m}=$ $\qquad$ $\mathrm{b}=$ $\qquad$ $f(x)=$

$\mathrm{m}=\ldots \quad \mathrm{b}=$ $\qquad$ $f(x)=$ $\qquad$

$\mathrm{m}=$ $\qquad$ $\mathrm{b}=$ $\qquad$ $\mathrm{f}(\mathrm{x})=$

$\mathrm{m}=$ $\qquad$ $\mathrm{b}=$ $\qquad$ $f(x)=$ $\qquad$

## Analyze the following functions:

1. $f(x)=1$

2. $f(x)=2$

3. $f(x)=-1$

4. $f(x)=0$

5. $f(x)=x$

6. $f(x)=x+1$

7. $f(x)=-x$


Domain: $\qquad$
Range: $\qquad$
Increase: $\qquad$
Decrease: $\qquad$
y intercept: (, )
x intercept: (, )
11. $f(x)=3-2 x$

| - | - |  | " |  |  | $\square$ |  | Domain: |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | - | - | - |  |  | - | - |  |
|  | - |  | - |  |  | - |  | Range: |
|  | - |  | - |  |  | - |  |  |
|  |  |  | 2 |  |  |  |  | Increase: |
| - | $\cdots$ | $\rightarrow$ |  | \% |  |  | i $: \times$ |  |
|  |  |  |  |  |  |  |  | Decrease: |
|  |  |  |  |  |  |  |  |  |
|  |  |  | $\rightarrow$ |  |  |  |  | y intercept: ( , ) |
|  |  |  |  |  |  | - |  |  |
|  |  |  | $-$ | - |  |  |  | $x$ intercept: ( , ) |


12. $\mathrm{f}(\mathrm{x})=\frac{x}{3}$

9. $f(x)=2 x$

| - | - | - | ${ }^{9}$ |  |  |  | Domain: |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | - | - | - |  |  |  |  |
|  | - |  | - |  |  |  | Range: |
|  | , | - | ${ }^{4}$ |  | - |  |  |
|  |  |  | -2 |  |  |  | Increase: |
| $\square$ | $\square$ | 7 |  |  | 4 | - ${ }^{\text {a }}$ - |  |
|  |  |  | $-2$ |  |  |  | Decrease: |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  | $y$ intercept: (, ) |
|  |  |  | ${ }^{-9}$ |  |  |  |  |
|  |  |  |  |  |  |  | $x$ intercept: (, ) |

13. $f(x)=2 x+1$

14. $f(x)=3 x-5$

| - | T | Domain: |
| :---: | :---: | :---: |
|  | - | Range: |
|  | - |  |
| ; - 7 | ; ; | Increase: |
|  | - | Decrease: |
|  | - | y intercept: (, ) |
|  | - | x intercept: (, ) |

14. $f(x)=2 x-2$

| - | - |  | - |  |  |  | - | Domain: |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | - |  |  |  |  |  |
| , |  |  | - |  |  |  |  | Range: |
|  |  |  | 4 |  |  |  |  | Range. |
|  |  |  | 2 |  |  |  |  | Increase: |
| - ${ }^{-1}$ | $\cdots-1$ | - |  | 2 | i | i | $\cdots \times$ |  |
|  | - |  | -2 |  |  |  |  | Decrease: |
|  | - |  |  |  |  | - |  |  |
|  |  |  |  |  |  |  |  | y intercept: ( , ) |
|  |  |  |  |  |  |  |  |  |
|  | - |  | $-8$ | - |  | , |  | $x$ intercept: ( , ) |

15. $f(x)=3 x+5$


Domain: $\qquad$
Range: $\qquad$
Increase: $\qquad$
Decrease: $\qquad$
y intercept: (, )
x intercept: ( , )
19. $f(x)=-\frac{3}{2} x-\frac{3}{2}$

20. $f(x)=-\frac{1}{2} x-\frac{3}{2}$

17. $\mathrm{f}(\mathrm{x})=\frac{x}{4}+6$

| $\square$ | , |  | ${ }^{4}$ | $\square$ | $\cdots$ | Domain: |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | - | - | - | - |  |  |
| - |  |  | - |  |  | Range: |
|  |  |  | - |  | - |  |
|  |  |  | 2 |  |  | Increase: |
| ${ }^{-9}$ | $\rightarrow$ |  |  | ; 1 | - $i^{\circ}$ |  |
|  |  |  |  |  | $\checkmark$ | Decrease: |
|  |  |  | -4 | - | , |  |
|  |  |  |  |  |  | $y$ intercept: (, ) |
|  |  |  |  |  | $\square$ |  |
|  |  |  | ${ }^{-8}$ | $\square$ | $\square$ | $x$ intercept: (, ) |

21. $\mathrm{f}(\mathrm{x})=\frac{7}{2} \mathrm{x}-\frac{1}{4}$

22. $f(x)=\frac{3}{2} x-5$

|  |  |  |  |  | $y$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  |  |
|  | , |  |  |  | - |  | - |  |  |  |
|  |  |  |  |  | $\cdot$ |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  | - |  | - |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  | -2 |  |  |  |  |  |
| ${ }^{-8}$ | $\stackrel{5}{5}$ | 4 | -2 |  |  | 2 | 4 |  | ¢ 1 |  |
|  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  | -- |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  | $-4$ |  |  |  |  |  |
|  |  |  |  |  | - |  |  |  |  |  |
|  |  |  |  |  | $-6$ |  |  |  |  |  |
|  |  |  |  |  | --8 |  |  |  |  |  |
|  |  |  |  |  | - |  |  |  |  |  |

Domain: $\qquad$
Range: $\qquad$
Increase: $\qquad$
Decrease: $\qquad$
y intercept: (, )
$x$ intercept: (, )
22. $\mathrm{f}(\mathrm{x})=-\frac{9}{5} \mathrm{x}+\frac{8}{3}$

|  | - | - | , | , |  |  | - |  | Domain: |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| - | - | , |  | - |  | - |  |  |  |
| - |  |  | - | - |  | , |  |  |  |
|  |  |  |  |  |  |  |  |  | Range: |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  | 2 | ${ }^{2}$, |  |  |  |  | Increase: |
| ${ }^{-9}$ |  | -2 |  |  |  | 4 ; | $\because \times$ |  |  |
|  |  |  |  | 2 |  | - |  |  | Decrease: |
|  |  |  |  | - |  |  | - |  |  |
|  |  |  |  |  |  |  |  |  | y intercept: ( , ) |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  | $x$ intercept: ( , ) |

23. $3 x+2 y=2$


Domain: $\qquad$
Range: $\qquad$
Increase: $\qquad$
Decrease: $\qquad$
y intercept: (, )
x intercept: (, )
24. $4 x-2 y-3=1$
Domain:
Range: $\qquad$
Increase: $\qquad$
Decrease $\qquad$
y intercept: ( , )
$x$ intercept: (, )
25. $-2 y+3 x=-5$


Domain: $\qquad$

Range: $\qquad$
Increase: $\qquad$
Decrease: $\qquad$
y intercept: (, )
x intercept: (, )
27. $y+2 x-3=1$

| $\square \square$ | - | Domain: |
| :---: | :---: | :---: |
|  | - |  |
| - | - | Range: |
| - | - |  |
|  | 2 | Increase: |
|  | \% i i i x |  |
|  | - | Decrease: |
| - | - |  |
|  | $\rightarrow$ | y intercept: (, ) |
|  | $\rightarrow$ | $x$ intercept: ( , ) |
|  |  | x intercept. ( , ) |

28. $5 y+5 x=5$

29. $2 x-2 y-3=1$

30. $\mathrm{y}-\mathrm{x}=2$

31. $\mathrm{x}-2 \mathrm{y}-150=0$

| $\square$ | - | - |  | $\square$ | - | Domain: |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | - |  |  |  |  |
|  |  | - |  |  |  | Range: |
| - | - | - |  | - |  |  |
|  |  | ${ }^{2}$ |  | - |  | Increase: |
| $\stackrel{-}{-8}$ | $\cdots-1-2$ |  | ${ }^{2}$ | i i | $\stackrel{*}{*}$ |  |
|  |  | -2 |  |  |  | Decrease: |
|  |  | - |  | - |  |  |
|  |  | $\rightarrow$ |  |  |  | $y$ intercept: ( , ) |
|  |  | - |  |  |  |  |
|  | $\cdots$ | ${ }^{\circ}$ |  |  |  | $x$ intercept: (, ) |

31. Write the equation of the line that has a slope of 2 and passes through the point $(2,4)$ in the forms: $y=m x+b$ and $a x+b y+c=0,(a, b \in Z)$

32. Write the equation of the line that has a slope of $-\frac{1}{2}$ and passes through the point $(-2,-3)$ in the forms: $y=m x+b$ and $a x+b y+c=0,(a, b \in Z)$

33. Write the equation of the line that has a slope of $-\frac{5}{2}$ and passes through the point $(-1,2)$ in the forms: $\mathrm{y}=\mathrm{mx}+\mathrm{b}$ and $\mathrm{ax}+\mathrm{by}+\mathrm{c}=0,(\mathrm{a}, \mathrm{b} \in Z)$

34. Find the equation of the line that passes through the points $(1,1),(2,4)$, indicate its y and x intercepts and sketch it. Write its equation in the forms: y $=m x+b$ and $a x+b y+c=0,(a, b \in Z)$

35. Find the equation of the line that passes through the points $(-1,-5),(4,3)$, indicate its y and x intercepts and sketch it. Write its equation in the forms: y $=m x+b$ and $a x+b y+c=0,(a, b \in Z)$

36. Find the equation of the line that passes through the points $(-5,1),(-2,4)$, indicate its y and x intercepts, sketch it and write it in both formas $\mathrm{y}=\mathrm{mx}+$ b and $\mathrm{ax}+\mathrm{by}+\mathrm{c}=0,(\mathrm{a}, \mathrm{b} \in Z)$

37. Write the equation of the line that is parallel to the line $y=5 x-2$ and passes through the point $(-2,-1)$. Write its equation in the forms: $\mathrm{y}=\mathrm{mx}+\mathrm{b}$ and ax $+b y+c=0,(a, b \in Z)$

38. Write the equation of the line that is parallel to the line $y=-0.5 x-1$ and passes through the point $(-3,6)$. Write its equation in the forms: $\mathrm{y}=\mathrm{mx}+$ b and $\mathrm{ax}+\mathrm{by}+\mathrm{c}=0,(\mathrm{a}, \mathrm{b} \in Z)$

39. Sketch and write the equation of the line with a slope of $-\frac{1}{5}$ that passes through the point $(0,2)$.

40. Sketch and write the equation of the lines with a slope: $1,2,-3,-1,-\frac{1}{2},-\frac{1}{3}$, that pass through the point $(0,0)$.

41. Sketch and write the equation of the line with a slope of -3 that passes through the point $(0,-3)$.

42. Sketch and write the equation of the line with a slope of 2 that passes through the point $(2,0)$

43. Sketch and write the equation of the line with a slope of $-\frac{1}{2}$ that passes through the point $(-2,0)$

44. Sketch and write the equation of the line with a slope of 2 that passes through the point $(-4,2)$

45. Find the intersection between the lines $f(x)=2 x-3$ and $f(x)=-5 x-2$
46. Find the intersection between the lines $f(x)=-12 x-13$ and $f(x)=15 x+20$.
47. Given the points $(1,2)$ and $(5,8)$. Find the distance between them. Find the midpoint. Sketch to illustrate your answer.

48. Given the points $(-3,2)$ and $(5,-6)$. Find the distance between them. Find the midpoint. Sketch to illustrate your answer.

49. Given the points $(-1,-6)$ and $(-5,-1)$. Find the distance between them. Find the midpoint. Sketch to illustrate your answer.


PERPENDICULAR LINES ( $\mathrm{m} \mathrm{m} \perp=-1$ )
50. Find the equation of a line perpendicular to the line $y=3 x-2$ that passes through the point $(3,12)$. Sketch to illustrate your answer.

51. Find all the lines perpendicular to the line $y=-3 x+4$. Fin the ones that passes through the point $(-3,1)$. Sketch to illustrate your answer.

52. Find a line perpendicular to the line $y=-\frac{2}{5} x+1$ that passes through the point $(-1,-7)$. Sketch to illustrate your answer.

53. Given that the slope of one of the lines is 3 and that the lines are perpendicular, find the exact coordinates of the point of intersection of the two lines.


## Application

1. The price of a new toy (in US\$) is $\mathrm{C}(\mathrm{t})=20-0.5 \mathrm{t}$, t given in days.
a. Sketch the corresponding graph.

b. What was the initial price of the toy? $\qquad$
c. Find the price of the toy after 10 days
d. What is the domain of the function, argument the answer,
e. What is the range of the function.
f. What is the meaning of 0.5 ? Does it have units? What are they?
2. You need to rent a car for one day and to compare the charges of 3 different companies. Company I charges $20 \$$ per day with additional cost of $0.20 \$$ per mile. Company II charges $30 \$$ per day with additional cost of $0.10 \$$ per mile. Company III charges $60 \$$ per day with no additional mileage charge.
a. Write the cost function for each one of the companies.
b. Sketch all 3 graphs on the same axes system.
c. Comment on the circumstances in which renting a car from each one of the companies is best.
